

1. a)  $x^2 - 2x = 35$   
 $\therefore x^2 - 2x - 35 = 0$  **M1**  
 $\therefore (x-7)(x+5) = 0$  **M1**  
 $\therefore x = 7$  or  $x = -5$  **A1**
- b)  $(x+2)^2 = -x$   
 $\therefore (x+2)(x+2) = -x$   
 $\therefore x^2 + 4x + 4 = -x$   
 $\therefore x^2 + 5x + 4 = 0$  **M1**  
 $\therefore (x+4)(x+1) = 0$  **M1**  
 $\therefore x = -4$  or  $x = -1$  **A1**
- c)  $x(x+1) = 6$   
 $\therefore x^2 + x = 6$   
 $\therefore x^2 + x - 6 = 0$  **M1**  
 $\therefore (x+3)(x-2) = 0$  **M1**  
 $\therefore x = -3$  or  $x = 2$  **A1**
- d)  $(x+3)(x+4) = x+4$   
 $\therefore x^2 + 3x + 4x + 12 = x + 4$   
 $\therefore x^2 + 7x + 12 = x + 4$   
 $\therefore x^2 + 6x + 8 = 0$  **M1**  
 $\therefore (x+4)(x+2) = 0$  **M1**  
 $\therefore x = -4$  or  $x = -2$  **A1**

[12 Marks]

2. a)  $a = 2, b = -3, c = -1$   

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(2)(-1)}}{2(2)} = \frac{3 \pm \sqrt{17}}{4}$$
 **M1**  
 $\therefore x = \frac{3 + \sqrt{17}}{4}$  or  $x = \frac{3 - \sqrt{17}}{4}$  **A1**

**Technique:** Use the quadratic formula:  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

- b)  $5x^2 = 2x + 3 \therefore 5x^2 - 2x - 3 = 0$  **M1**  
 $a = 5, b = -2, c = -3$   

$$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(5)(-3)}}{2(5)} = \frac{2 \pm \sqrt{4 + 60}}{10} = \frac{2 \pm \sqrt{64}}{10} = \frac{2 \pm 8}{10}$$
 **M1**

**Technique:** Rearrange the equation into the form  $ax^2 + bx + c = 0$  first

- $\therefore x = -\frac{3}{5}$  or  $x = 1$  **A1**
- c)  $(2x+3)^2 = (2x+3)(2x+3) = 8$  **M1**  
 $\therefore 4x^2 + 6x + 6x + 9 = 8$   
 $\therefore 4x^2 + 12x + 1 = 0$  **M1**  
 $a = 4, b = 12, c = 1$   

$$x = \frac{-12 \pm \sqrt{12^2 - 4(4)(1)}}{2(4)} = \frac{-12 \pm \sqrt{144 - 16}}{8}$$
  

$$= \frac{-12 \pm \sqrt{128}}{8} = \frac{-12 \pm 8\sqrt{2}}{8} = \frac{-3 \pm 2\sqrt{2}}{2}$$
 **M1**  
 $\therefore x = \frac{-3 + 2\sqrt{2}}{2}$  or  $x = \frac{-3 - 2\sqrt{2}}{2}$  **A1**

**Technique:** Rearrange the equation into the form  $ax^2 + bx + c = 0$  first

[7 Marks]

$$3. \quad a) \quad x^2 - 4x + 4 = \left(x - \frac{4}{2}\right)^2 - \left(\frac{4}{2}\right)^2 + 4 \quad \leftarrow$$

$$= (x-2)^2 - 2^2 + 4 = (x-2)^2 = 0 \quad \mathbf{M1}$$

$$\therefore x = 2 \quad (\text{one repeated root}) \quad \mathbf{A1}$$

**Technique:** Halve the coefficient of  $x$  and then take away its square, i.e.

$$x^2 + ax = \left(x + \frac{a}{2}\right)^2 - \left(\frac{a}{2}\right)^2$$

$$b) \quad x^2 + 6x + 3 = (x+3)^2 - 3^2 + 3 = 0$$

$$\therefore (x+3)^2 - 6 = 0 \quad \mathbf{M1}$$

$$\therefore (x+3)^2 = 6$$

$$\therefore x+3 = \pm\sqrt{6}$$

$$\therefore x = -3 + \sqrt{6} \quad \text{or} \quad x = -3 - \sqrt{6} \quad \mathbf{A1}$$

$$c) \quad x^2 + 5x - 1 = 0$$

$$\left(x + \frac{5}{2}\right)^2 - \left(\frac{5}{2}\right)^2 - 1 = 0$$

$$\left(x + \frac{5}{2}\right)^2 - \frac{25}{4} - 1 = 0$$

$$\left(x + \frac{5}{2}\right)^2 - \frac{29}{4} = 0$$

$$\left(x + \frac{5}{2}\right)^2 = \frac{29}{4} \quad \mathbf{M1}$$

$$\therefore x + \frac{5}{2} = \pm\sqrt{\frac{29}{4}} = \pm\frac{\sqrt{29}}{2}$$

$$\therefore x = -\frac{5}{2} \pm \frac{\sqrt{29}}{2}$$

$$\therefore x = -\frac{5}{2} + \frac{\sqrt{29}}{2} \quad \text{or} \quad x = -\frac{5}{2} - \frac{\sqrt{29}}{2} \quad \mathbf{A1} \quad [6 \text{ Marks}]$$

$$4. \quad x^2 + 2x - 5 = \left(x + \frac{2}{2}\right)^2 - \left(\frac{2}{2}\right)^2 - 5 \quad \mathbf{M1}$$

$$= (x+1)^2 - 1^2 - 5 = (x+1)^2 - 1 - 5$$

$$= (x+1)^2 - 6 \quad (\text{where } p=1, q=1 \text{ and } r=-6) \quad \mathbf{A1} \quad [2 \text{ Marks}]$$

$$5. \quad 2x^2 - 4x + 8 = 2(x^2 - 2x) + 8$$

$$= 2((x-1)^2 - 1^2) + 8 \quad \mathbf{M1}$$

$$= 2(x-1)^2 - 2 + 8$$

$$= 2(x-1)^2 + 6 \quad (\text{where } p=2, q=-1 \text{ and } r=6) \quad \mathbf{A1} \quad [2 \text{ Marks}]$$

$$6. \quad a) \quad f(x) = 3x - 15 \therefore f(2) = 3(2) - 15 = 6 - 15 = -9 \quad \mathbf{A1}$$

$$g(x) = x^2 + 11x + 1 \therefore g(5) = 5^2 + 11(5) + 1 = 25 + 55 + 1 = 81 \quad \mathbf{A1}$$

$$b) \quad f(x) = g(x)$$

$$3x - 15 = x^2 + 11x + 1$$

$$\therefore x^2 + 11x - 3x + 1 + 15 = 0$$

$$\therefore x^2 + 8x + 16 = 0 \quad \mathbf{M1}$$

$$\therefore (x+4)(x+4) = 0 \quad \mathbf{M1}$$

$$\therefore x = -4 \quad (\text{one repeated root}) \quad \mathbf{A1} \quad [5 \text{ Marks}]$$

7. a)  $a = 5, b = 12, c = 8$   
 $b^2 - 4ac = 12^2 - 4(5)(8)$   
 $= 144 - 160 = -16$  **A1**  
 $-16 < 0 \therefore$  no real roots **A1**
- b)  $g(x) = (-x + 6)(2x + 3)$   
 $= -2x^2 - 3x + 12x + 18$   
 $= -2x^2 + 9x + 18$  **M1**  
 $a = -2, b = 9, c = 18$   
 $b^2 - 4ac = 9^2 - 4(-2)(18) = 81 + 144 = 225$  **A1**  
 $225 > 0 \therefore$  two real roots **A1**
- c)  $a = 3, b = -6, c = 2$   
 $b^2 - 4ac = (-6)^2 - 4(3)(2) = 36 - 24 = 12$  **A1**  
 $12 > 0 \therefore$  two real roots **A1**
- d)  $j(x) = (2x + 8)(3x - 4) = 6x^2 - 8x + 24x - 32$   
 $= 6x^2 + 16x - 32$  **M1**  
 $a = 6, b = 16, c = -32$   
 $b^2 - 4ac = 16^2 - 4(6)(-32) = 256 + 768 = 1024$  **A1**  
 $1024 > 0 \therefore$  two real roots **A1** **[10 Marks]**

8.  $2x = \sqrt{4x + 3}$   
 $\therefore 4x^2 = 4x + 3$   
 $\therefore 4x^2 - 4x - 3 = 0$  **M1**  
 $a = 4, b = -4, c = -3$   

$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(4)(-3)}}{2(4)} = \frac{4 \pm \sqrt{16 + 48}}{8} = \frac{4 \pm \sqrt{64}}{8} = \frac{4 \pm 8}{8}$$
 **M1**  
 $\therefore x = \frac{3}{2}$  or  $x = -\frac{1}{2}$  (both solutions allowed as  $x > -\frac{3}{4}$ ) **A1** **[3 Marks]**

9.  $a = 1, b = k, c = 4$   
 $b^2 - 4ac = 0$  for one repeated root **M1**  
 So there is one repeated root if  $k^2 - 4(1)(4) = 0$  **M1**  
 $\therefore k^2 = 16 \therefore k = \pm 4$   
 $\therefore k = 4$  or  $k = -4$  **A1** **[3 Marks]**

10.  $a = 2, b = -5, c = A$   
 $b^2 - 4ac = 0$  for one solution **M1**  
 So there is one solution if  $(-5)^2 - 4(2)A = 0$  **M1**  
 $\therefore 25 = 8A$   
 $\therefore A = \frac{25}{8}$  **A1** **[3 Marks]**

**TOTAL 53 MARKS**