

Subtopics: Solving quadratic equations, completing the square, functions, quadratic graphs, discriminants, modelling

1. Rearrange the following equations into the form $x^2 + bx + c = 0$, then solve by **factorisation**:
 - a) $x^2 - 2x = 35$
 - b) $(x + 2)^2 = -x$
 - c) $x(x + 1) = 6$
 - d) $(x + 3)(x + 4) = x + 4$

[12]

2. Solve the following equations using the **quadratic formula**, leaving your answers in simplified surd form when necessary:
 - a) $2x^2 - 3x - 1 = 0$
 - b) $5x^2 = 2x + 3$
 - c) $(2x + 3)^2 = 8$

[7]

3. Solve by **completing the square**, leaving your answers in simplified surd form when necessary:
 - a) $x^2 - 4x + 4 = 0$
 - b) $x^2 + 6x + 3 = 0$
 - c) $x^2 + 5x - 1 = 0$

[6]

4. Write $x^2 + 2x - 5$ in the form $p(x + q)^2 + r$ where p , q and r are integers.

[2]

5. Write $2x^2 - 4x + 8$ in the form $p(x + q)^2 + r$ where p , q and r are integers.

[2]

6. The functions f and g are given by $f(x) = 3x - 15$ and $g(x) = x^2 + 11x + 1$
 - a) Find the values of $f(2)$ and $g(5)$ **[2]**
 - b) Find the value of x where $f(x) = g(x)$ **[3]**

7. Calculate the value of the **discriminant** for the following functions, then state whether the function has two real roots, no real roots or one repeated root:
 - a) $f(x) = 5x^2 + 12x + 8$
 - b) $g(x) = (-x + 6)(2x + 3)$
 - c) $h(x) = 3x^2 - 6x + 2$
 - d) $j(x) = (2x + 8)(3x - 4)$

[10]

8. Solve $2x = \sqrt{4x + 3}$, where $x \geq -\frac{3}{4}$, by first squaring both sides and then using the **quadratic formula**.

[3]

9. Find the values of k for which $f(x) = x^2 + kx + 4$ has **one** repeated root.

[3]

10. Find the value of A for which $2x^2 - 5x + A = 0$ has exactly **one** solution.

[3]

TOTAL 53 MARKS