



WILMSLOW
HIGH SCHOOL

A level Mathematics
Year 11 to 12 transition

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Expanding brackets and simplifying expressions

Answers

- 1** **a** $6x - 3$ **b** $-10pq - 8q^2$
 c $-3xy + 2y^2$
- 2** **a** $21x + 35 + 12x - 48 = 33x - 13$
 b $40p - 16 - 12p - 27 = 28p - 43$
 c $27s + 9 - 30s + 50 = -3s + 59 = 59 - 3s$
 d $8x - 6 - 3x - 5 = 5x - 11$
- 3** **a** $12x^2 + 24x$ **b** $20k^3 - 48k$
 c $10h - 12h^3 - 22h^2$ **d** $21s^2 - 21s^3 - 6s$
- 4** **a** $-y^2 - 4$ **b** $5x^2 - 11x$
 c $2p - 7p^2$ **d** $6b^2$
- 5** $y - 4$
- 6** **a** $-1 - 2m$ **b** $5p^3 + 12p^2 + 27p$
- 7** $7x(3x - 5) = 21x^2 - 35x$
- 8** **a** $x^2 + 9x + 20$ **b** $x^2 + 10x + 21$
 c $x^2 + 5x - 14$ **d** $x^2 - 25$
 e $2x^2 + x - 3$ **f** $6x^2 - x - 2$
 g $10x^2 - 31x + 15$ **h** $12x^2 + 13x - 14$
 i $18x^2 + 39xy + 20y^2$ **j** $x^2 + 10x + 25$
 k $4x^2 - 28x + 49$ **l** $16x^2 - 24xy + 9y^2$
- 9** $2x^2 - 2x + 25$
- 10** **a** $x^2 - 1 - \frac{2}{x^2}$ **b** $x^2 + 2 + \frac{1}{x^2}$

Factorising expressions

Answers

- 1** **a** $2x^3y^3(3x - 5y)$ **b** $7a^3b^2(3b^3 + 5a^2)$
 c $5x^2y^2(5 - 2x + 3y)$
- 2** **a** $(x + 3)(x + 4)$ **b** $(x + 7)(x - 2)$
 c $(x - 5)(x - 6)$ **d** $(x - 8)(x + 3)$
 e $(x - 9)(x + 2)$ **f** $(x + 5)(x - 4)$
 g $(x - 8)(x + 5)$ **h** $(x + 7)(x - 4)$
- 3** **a** $(6x - 7y)(6x + 7y)$ **b** $(2x - 9y)(2x + 9y)$
 c $2(3a - 10bc)(3a + 10bc)$
- 4** **a** $(x - 1)(2x + 3)$ **b** $(3x + 1)(2x + 5)$
 c $(2x + 1)(x + 3)$ **d** $(3x - 1)(3x - 4)$
 e $(5x + 3)(2x + 3)$ **f** $2(3x - 2)(2x - 5)$
- 5** **a** $\frac{2(x+2)}{x-1}$ **b** $\frac{x}{x-1}$
 c $\frac{x+2}{x}$ **d** $\frac{x}{x+5}$
 e $\frac{x+3}{x}$ **f** $\frac{x}{x-5}$
- 6** **a** $\frac{3x+4}{x+7}$ **b** $\frac{2x+3}{3x-2}$
 c $\frac{2-5x}{2x-3}$ **d** $\frac{3x+1}{x+4}$
- 7** $(x + 5)$
- 8** $\frac{4(x+2)}{x-2}$

Rules of indices

Answers

1	a	1	b	1	c	1	d	1
2	a	7	b	4	c	5	d	2
3	a	125	b	32	c	343	d	8
4	a	$\frac{1}{25}$	b	$\frac{1}{64}$	c	$\frac{1}{32}$	d	$\frac{1}{36}$
5	a	$\frac{3x^3}{2}$	b	$5x^2$				
	c	$3x$	d	$\frac{y}{2x^2}$				
	e	$y^{\frac{1}{2}}$	f	c^{-3}				
	g	$2x^6$	h	x				
6	a	$\frac{1}{2}$	b	$\frac{1}{9}$	c	$\frac{8}{3}$		
	d	$\frac{1}{4}$	e	$\frac{4}{3}$	f	$\frac{16}{9}$		
7	a	x^{-1}	b	x^{-7}	c	$x^{\frac{1}{4}}$		
	d	$x^{\frac{2}{5}}$	e	$x^{\frac{1}{3}}$	f	$x^{\frac{2}{3}}$		
8	a	$\frac{1}{x^3}$	b	1	c	$\sqrt[5]{x}$		
	d	$\sqrt[5]{x^2}$	e	$\frac{1}{\sqrt{x}}$	f	$\frac{1}{\sqrt[4]{x^3}}$		
9	a	$5x^{\frac{1}{2}}$	b	$2x^{-3}$	c	$\frac{1}{3}x^{-4}$		
	d	$2x^{-\frac{1}{2}}$	e	$4x^{\frac{1}{3}}$	f	$3x^0$		
10	a	$x^3 + x^{-2}$	b	$x^3 + x$	c	$x^{-2} + x^{-7}$		

Surds

Answers

1 a $3\sqrt{5}$
c $4\sqrt{3}$
e $10\sqrt{3}$
g $6\sqrt{2}$

b $5\sqrt{5}$
d $5\sqrt{7}$
f $2\sqrt{7}$
h $9\sqrt{2}$

2 a $15\sqrt{2}$
c $3\sqrt{2}$
e $6\sqrt{7}$

b $\sqrt{5}$
d $\sqrt{3}$
f $5\sqrt{3}$

3 a -1
c $10\sqrt{5}-7$

b $9-\sqrt{3}$
d $26-4\sqrt{2}$

4 a $\frac{\sqrt{5}}{5}$
c $\frac{2\sqrt{7}}{7}$
e $\sqrt{2}$
g $\frac{\sqrt{3}}{3}$

b $\frac{\sqrt{11}}{11}$
d $\frac{\sqrt{2}}{2}$
f $\sqrt{5}$
h $\frac{1}{3}$

5 a $\frac{3+\sqrt{5}}{4}$

b $\frac{2(4-\sqrt{3})}{13}$

c $\frac{6(5+\sqrt{2})}{23}$

6 $x-y$

7 a $3+2\sqrt{2}$

b $\frac{\sqrt{x}+\sqrt{y}}{x-y}$

Rearranging equations

Answers

1 $d = \frac{C}{\pi}$

2 $w = \frac{P-2l}{2}$

3 $T = \frac{S}{D}$

4 $t = \frac{q-r}{p}$

5 $t = \frac{2u}{2a-1}$

6 $x = \frac{V}{a+4}$

7 $y = 2 + 3x$

8 $a = \frac{3x+1}{x+2}$

9 $d = \frac{b-c}{x}$

10 $g = \frac{2h+9}{7-h}$

11 $e = \frac{1}{x+7}$

12 $x = \frac{4y-3}{2+y}$

13 a $r = \sqrt{\frac{A}{\pi}}$

b $r = \sqrt[3]{\frac{3V}{4\pi}}$

a $r = \frac{P}{\pi+2}$

b $r = \sqrt{\frac{3V}{2\pi h}}$

14 a $x = \frac{abz}{cdy}$

b $x = \frac{3dz}{4\pi cpy^2}$

15 $\sin B = \frac{b \sin A}{a}$

16 $\cos B = \frac{a^2 + c^2 - b^2}{2ac}$

17 a $x = \frac{q+pt}{q-ps}$

b $x = \frac{3py+2pqy}{3p-apq} = \frac{y(3+2q)}{3-aq}$

Completing the square

Answers

1 a $(x+2)^2 - 1$

b $(x-5)^2 - 28$

c $(x-4)^2 - 16$

d $(x+3)^2 - 9$

e $(x-1)^2 + 6$

f $\left(x + \frac{3}{2}\right)^2 - \frac{17}{4}$

2 a $2(x-2)^2 - 24$

b $4(x-1)^2 - 20$

c $3(x+2)^2 - 21$

d $2\left(x + \frac{3}{2}\right)^2 - \frac{25}{2}$

3 a $2\left(x + \frac{3}{4}\right)^2 + \frac{39}{8}$

b $3\left(x - \frac{1}{3}\right)^2 - \frac{1}{3}$

c $5\left(x + \frac{3}{10}\right)^2 - \frac{9}{20}$

d $3\left(x + \frac{5}{6}\right)^2 + \frac{11}{12}$

4 $(5x+3)^2 + 3$

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Solving quadratic equations by factorisation

Answers

- 1**
- | | | | |
|----------|-------------------------------|----------|-------------------------------|
| a | $x = 0$ or $x = -\frac{2}{3}$ | b | $x = 0$ or $x = \frac{3}{4}$ |
| c | $x = -5$ or $x = -2$ | d | $x = 2$ or $x = 3$ |
| e | $x = -1$ or $x = 4$ | f | $x = -5$ or $x = 2$ |
| g | $x = 4$ or $x = 6$ | h | $x = -6$ or $x = 6$ |
| i | $x = -7$ or $x = 4$ | j | $x = 3$ |
| k | $x = -\frac{1}{2}$ or $x = 4$ | l | $x = -\frac{2}{3}$ or $x = 5$ |
- 2**
- | | | | |
|----------|--------------------------------|----------|-------------------------------|
| a | $x = -2$ or $x = 5$ | b | $x = -1$ or $x = 3$ |
| c | $x = -8$ or $x = 3$ | d | $x = -6$ or $x = 7$ |
| e | $x = -5$ or $x = 5$ | f | $x = -4$ or $x = 7$ |
| g | $x = -3$ or $x = 2\frac{1}{2}$ | h | $x = -\frac{1}{3}$ or $x = 2$ |

Solving quadratic equations by completing the square

Answers

3 a $x = 2 + \sqrt{7}$ or $x = 2 - \sqrt{7}$ b $x = 5 + \sqrt{21}$ or $x = 5 - \sqrt{21}$

c $x = -4 + \sqrt{21}$ or $x = -4 - \sqrt{21}$ d $x = 1 + \sqrt{7}$ or $x = 1 - \sqrt{7}$

$$\sqrt{6.5}$$

e $x = -2 +$

4 a $x = 1 + \sqrt{14}$

c $x = \frac{5 + \sqrt{13}}{2}$

$$\text{or } x = -2 - \sqrt{6.5}$$

$$\text{or } x = 1 - \text{or } x = \sqrt{14}$$

$$\frac{5 - \sqrt{13}}{2}$$

f $x =$

b $x =$

$$\frac{-3 + \sqrt{89}}{10}$$

$$\frac{-3 + \sqrt{23}}{2}$$

or $x =$

or $x =$

$$\frac{-3 - 89}{10}$$

$$\frac{\sqrt{\quad}}{\quad}$$

$$\frac{-3 - 23}{2}$$

$$\frac{\sqrt{\quad}}{\quad}$$

Solving quadratic equations by using the formula

Answers

5 a $x = -1 + \frac{\sqrt{3}}{3}$ or $x = -1 - \frac{\sqrt{3}}{3}$ b $x = 1 + \frac{3\sqrt{2}}{2}$ or $x = 1 - \frac{3\sqrt{2}}{2}$

6 $x = \frac{7+\sqrt{41}}{2}$ or $x = \frac{7-\sqrt{41}}{2}$

7 $x = \frac{-3+\sqrt{89}}{20}$ or $x = \frac{-3-\sqrt{89}}{20}$

8 a $x = \frac{7+\sqrt{17}}{8}$ or $x = \frac{7-\sqrt{17}}{8}$

b $x = -1 + \sqrt{10}$ or $x = -1 - \sqrt{10}$

c $x = -1\frac{2}{3}$ or $x = 2$

$\frac{\sqrt{\quad}}{\quad}$

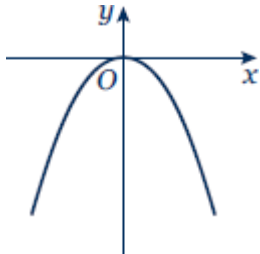
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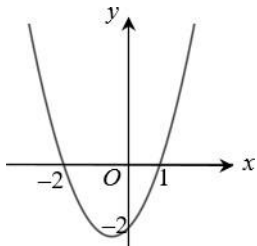
Sketching quadratic graphs

Answers

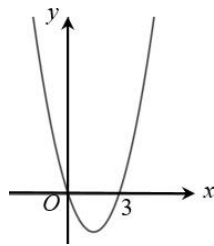
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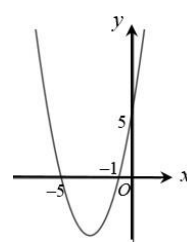
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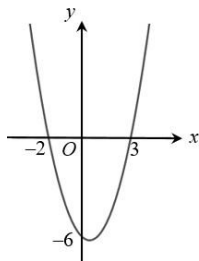
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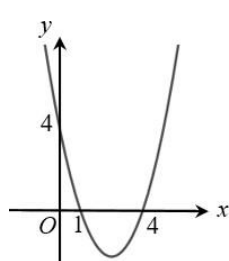
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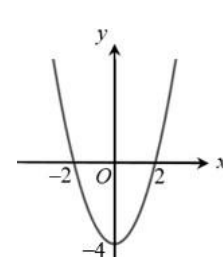
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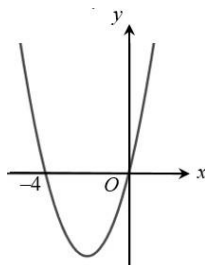
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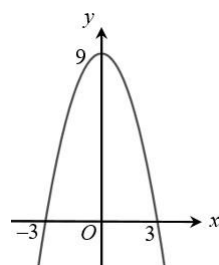
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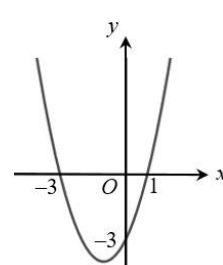
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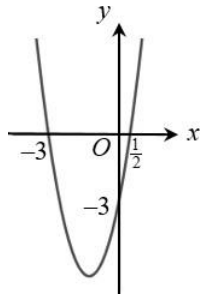
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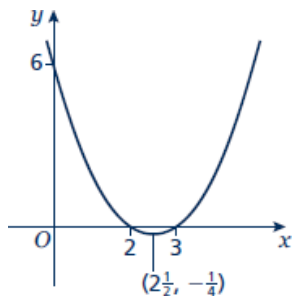
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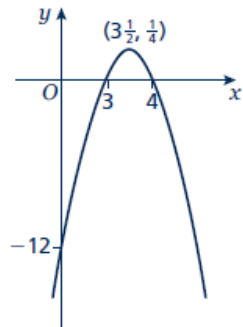
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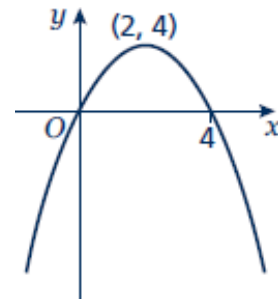
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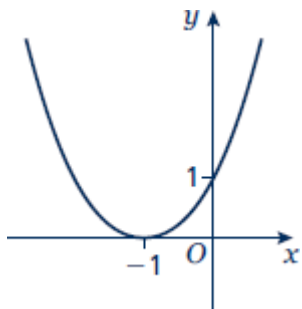
b



c



6



Line of symmetry at $x = -1$.

Solving linear simultaneous equations by elimination

Answers

1 $x = 1, y = 4$

2 $x = 3, y = -2$

3 $x = 2, y = -5$

4 $x = 3, y = -\frac{1}{2}$

5 $x = 6, y = -1$

6 $x = -2, y = 5$

Solving linear simultaneous equations by substitution

Answers

7 $x = 9, y = 5$

8 $x = -2, y = -7$

9 $x = \frac{1}{2}, y = 3\frac{1}{2}$

10 $x = \frac{1}{2}, y = 3$

11 $x = -4, y = 5$

12 $x = -2, y = -5$

13 $x = \frac{1}{4}, y = 1\frac{3}{4}$

14 $x = -2, y = 2\frac{1}{2}$

15 $x = -2\frac{1}{2}, y = 5\frac{1}{2}$

Solving linear and quadratic simultaneous equations

Answers

1 $x = 1, y = 3$

$$x = -\frac{9}{5}, y = -\frac{13}{5}$$

2 $x = 2, y = 4$

$$x = 4, y = 2$$

3 $x = 1, y = -2$

$$x = 2, y = -1$$

4 $x = 4, y = 1$

$$x = \frac{16}{5}, y = \frac{13}{5}$$

5 $x = 3, y = 4$

$$x = 2, y = 1$$

6 $x = 7, y = 2$

$$x = -1, y = -6$$

7 $x = 0, y = 5$

$$x = -5, y = 0$$

8 $x = -\frac{8}{3}, y = -\frac{19}{3}$

$$x = 3, y = 5$$

9 $x = -2, y = -4$

$$x = 2, y = 4$$

10 $x = \frac{5}{2}, y = 6$

$$x = 3, y = 5$$

11 $x = \frac{1+\sqrt{5}}{2}, y = \frac{-1+\sqrt{5}}{2}$

$$x = \frac{1-\sqrt{5}}{2}, y = \frac{-1-\sqrt{5}}{2}$$

12 $x = \frac{-1+\sqrt{7}}{2}, y = \frac{3+\sqrt{7}}{2}$

$$x = \frac{-1-\sqrt{7}}{2}, y = \frac{3-\sqrt{7}}{2}$$

Solving simultaneous equations graphically

Answers

- 1**
- a** $x = 2, y = 5$
 - b** $x = 2, y = -3$
 - b** $x = -0.5, y = 2.5$
- 2**
- a** $x = -2, y = 2$
 - b** $x = 0.5, y = 0.5$
 - c** $x = -1, y = -2$
- 3**
- a** $x = 1, y = 0$ and $x = 4, y = 3$
 - b** $x = -2, y = 7$ and $x = 2, y = -5$
 - c** $x = -2, y = 5$ and $x = -1, y = 4$
- 4** $x = -3, y = 4$ and $x = 4, y = -3$
- 5**
- a**
 - i** $x = 2.5, y = -2$ and $x = -0.5, y = 4$
 - ii** $x = 2.41, y = -1.83$ and $x = -0.41, y = 3.83$
 - b** Solving algebraically gives the more accurate solutions as the solutions from the graph are only estimates, based on the accuracy of your graph.

Linear inequalities

Answers

- 1** **a** $x > 4$ **b** $x \leq 2$ **c** $x \leq -1$
 d $x > -\frac{7}{2}$ **e** $x \geq 10$ **f** $x < -15$
- 2** **a** $x < -20$ **b** $x \leq 3.5$ **c** $x < 4$
- 3** **a** $x \leq -4$ **b** $-1 \leq x < 5$ **c** $x \leq 1$
 d $x < -3$ **e** $x > 2$ **f** $x \leq -6$
- 4** **a** $t < \frac{5}{2}$ **b** $n \geq \frac{7}{5}$
- 5** **a** $x < -6$ **b** $x < \frac{3}{2}$
- 6** $x > 5$ (which also satisfies $x > 3$)

Quadratic inequalities

Answers

1 $-7 \leq x \leq 4$

2 $x \leq -2$ or $x \geq 6$

3 $\frac{1}{2} < x < 3$

4 $x < -\frac{3}{2}$ or $x > \frac{1}{2}$

5 $-3 \leq x \leq 4$

6 $-3 \leq x \leq 2$

7 $2 < x < 2\frac{1}{2}$

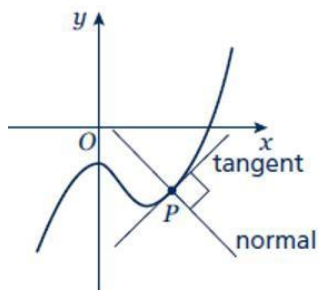
8 $x \leq -\frac{3}{2}$ or $x \geq \frac{5}{3}$

Sketching cubic and reciprocal graphs

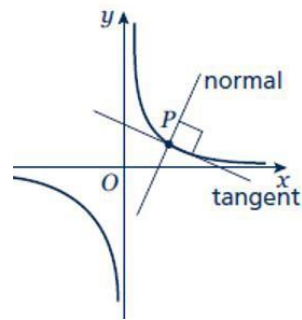
Answers

- 1 a i - C
ii - E
iii - B
iv - A
v - F
vi - D

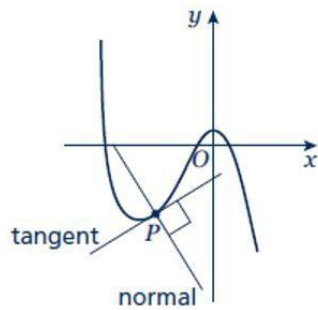
b ii



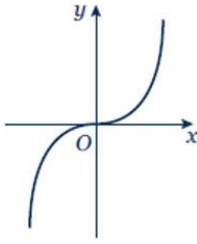
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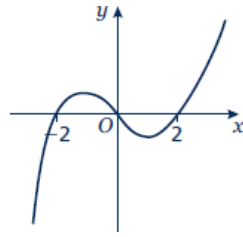
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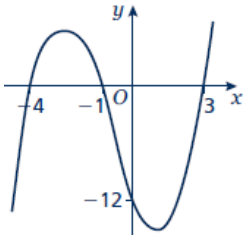
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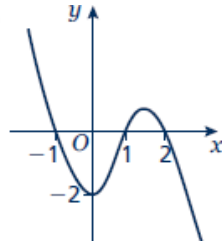
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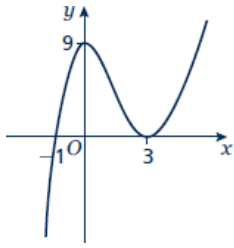
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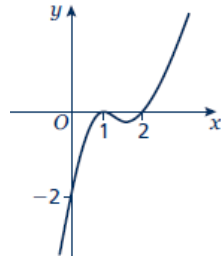
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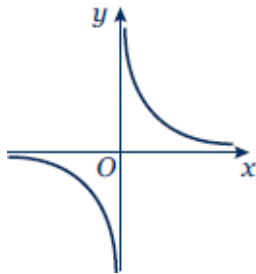
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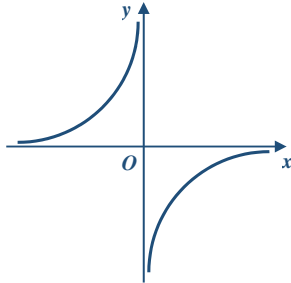
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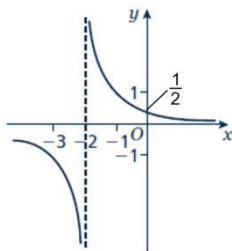
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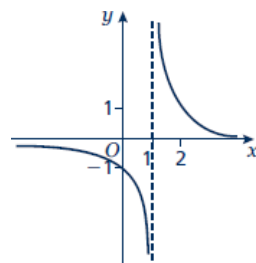
9



10



11

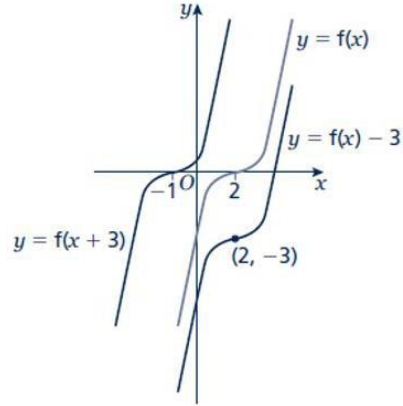
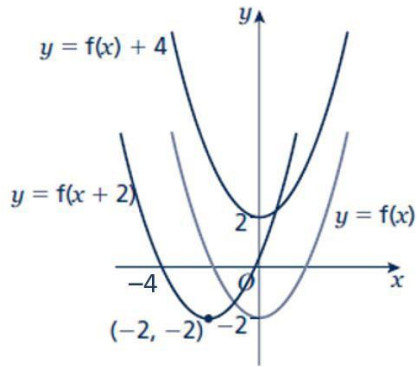


Translating graphs

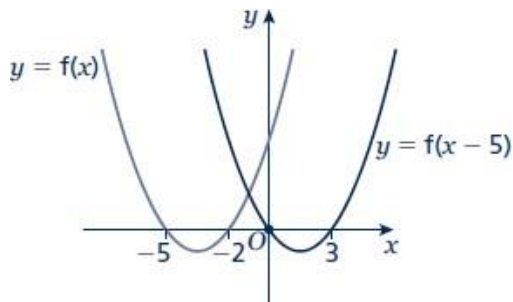
Answers

1

2



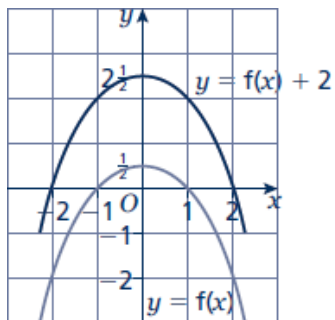
3



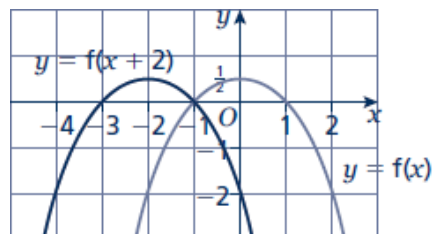
- 4** $C_1: y = f(x - 90^\circ)$
 $C_2: y = f(x) - 2$

- 5** $C_1: y = f(x - 5)$
 $C_2: y = f(x) - 3$

6 a



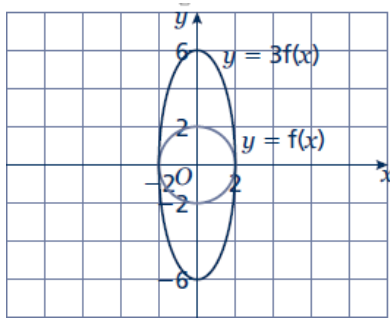
b



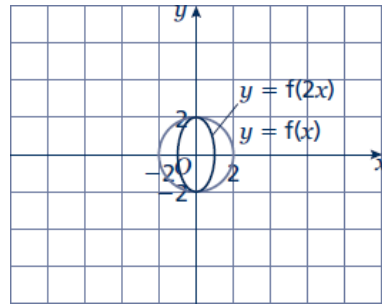
Stretching graphs

Answers

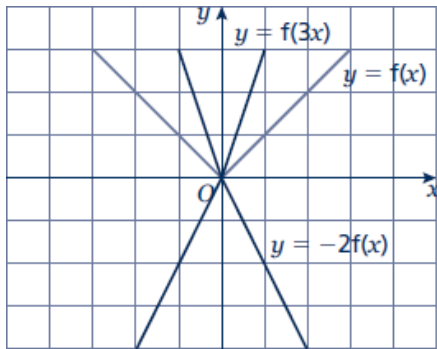
1 a



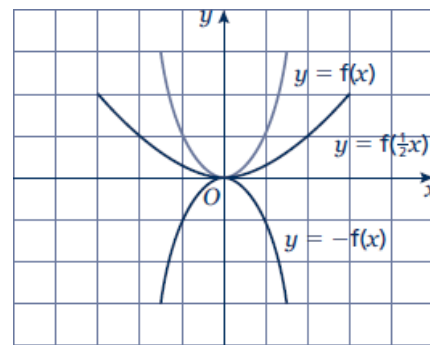
b



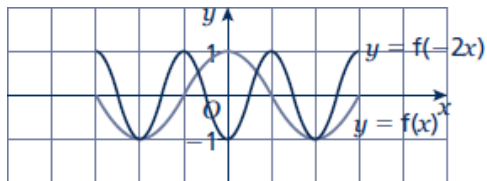
8



9



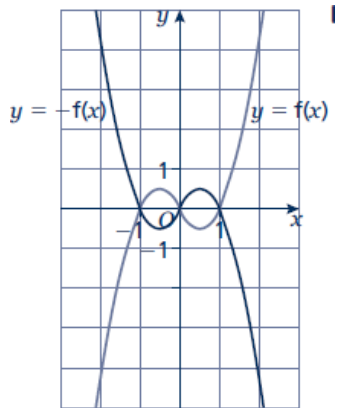
10



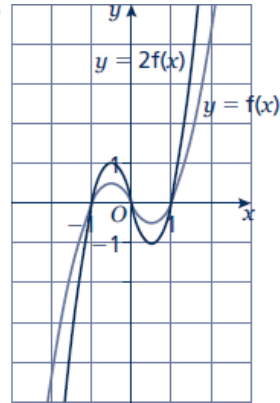
11 $y = f(2x)$

12 $y = -2f(2x)$ or $y = 2f(-2x)$

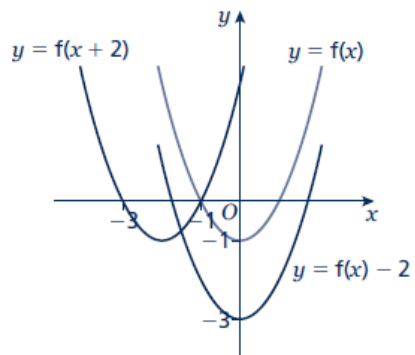
13 a



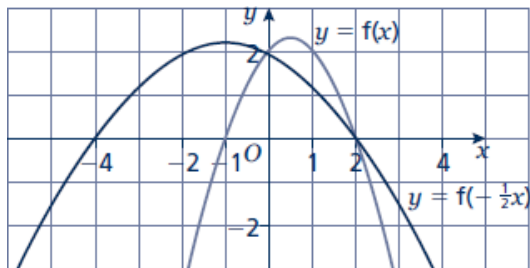
b



14



15



Straight line graphs

Answers

- 1 **a** $m = 3, c = 5$ **b** $m = -\frac{1}{2}, c = -7$
 c $m = 2, c = -\frac{3}{2}$ **b** $m = -1, c = 5$
 e $m = \frac{2}{3}, c = -\frac{7}{3}$ or $-2\frac{1}{3}$ **f** $m = -5, c = 4$

2

Gradient	y-intercept	Equation of the line
5	0	$y = 5x$
-3	2	$y = -3x + 2$
4	-7	$y = 4x - 7$

- 3 **a** $x + 2y + 14 = 0$ **b** $2x - y = 0$
 c $2x - 3y + 12 = 0$ **d** $6x + 5y + 10 = 0$

4 $y = 4x - 3$

5 $y = -\frac{2}{3}x + 7$

6 **a** $y = 2x - 3$ **b** $y = -\frac{1}{2}x + 6$

c $y = 5x - 2$ **d** $y = -3x + 19$

7 $y = -\frac{3}{2}x + 3$, the gradient is $-\frac{3}{2}$ and the y-intercept is 3.

The line intercepts the axes at (0, 3) and (2, 0).

Students may sketch the line or give coordinates that lie on the line such as $\left(1, \frac{3}{2}\right)$ or $(4, -3)$.

Parallel and perpendicular lines

Answers

1 a $y = 3x - 7$

b $y = -2x + 5$

c $y = -\frac{1}{2}x$

d $y = \frac{3}{2}x + 8$

2 $y = -2x - 7$

3 a $y = -\frac{1}{2}x + 2$

b $y = 3x + 7$

c $y = -4x + 35$

d $y = \frac{5}{2}x - 8$

4 a $y = -\frac{1}{2}x$

b $y = 2x$

5 a Parallel

b Neither

c Perpendicular

d Perpendicular

e Neither

f Parallel

6 a $x + 2y - 4 = 0$

b $x + 2y + 2 = 0$

c $y = 2x$

Volume and surface area of 3D solids

Answers

- 1**
- | | | | |
|----------|-----------------------------|----------|--------------------------------------|
| a | $V = 396 \text{ cm}^3$ | b | $V = 75\,000 \text{ cm}^3$ |
| c | $V = 402.5 \text{ cm}^3$ | d | $V = 200\pi \text{ cm}^3$ |
| e | $V = 1008\pi \text{ cm}^3$ | f | $V = \frac{1372}{3}\pi \text{ cm}^3$ |
| g | $V = 121.5\pi \text{ cm}^3$ | h | $V = 18\pi \text{ cm}^3$ |
| i | $V = 48\pi \text{ cm}^3$ | j | $V = \frac{98}{3}\pi \text{ cm}^3$ |
- 2** 17 cm
- 3** 17 cm
- 4** $V = x^3 + \frac{17}{2}x^2 + 4x$
- 5** 60 cm^3
- 6** 21.4 cm
- 7** 32 : 9
- 8** $r = \sqrt[3]{36x}$

Pythagoras' theorem

Answers

- 1** **a** 10.3 cm **b** 7.07 cm
 c 58.6 mm **d** 8.94 cm
- 2** **a** $4\sqrt{3}$ cm **b** $2\sqrt{21}$ cm
 c $8\sqrt{17}$ mm **d** $18\sqrt{5}$ mm
- 3** **a** $18\sqrt{13}$ mm **b** $2\sqrt{145}$ mm
 c $42\sqrt{2}$ mm **d** $6\sqrt{89}$ mm
- 4** 95.3 mm
- 5** $64\sqrt{10}$ km
- 6** $3\sqrt{5}$ units
- 7** $4\sqrt{3}$ cm

Trigonometry in right-angled triangles

Answers

- 1** **a** 6.49 cm **b** 6.93 cm **c** 2.80 cm
 d 74.3 mm **e** 7.39 cm **f** 6.07 cm
- 2** **a** 36.9° **b** 57.1° **c** 47.0° **d** 38.7°
- 3** 5.71 cm
- 4** 20.4°
- 5** **a** 45° **b** 1 cm **c** 30° **d** $\sqrt{3}$ cm

The cosine rule

Answers

6 **a** 6.46 cm **b** 9.26 cm **c** 70.8 mm **d** 9.70 cm

7 **a** 22.2° **b** 52.9° **c** 122.9° **d** 93.6°

8 **a** 13.7 cm **b** 76.0°

√ _____

The sine rule

Answers

9 **a** 4.33 cm **b** 15.0 cm **c** 45.2 mm **d** 6.39 cm

10 **a** 42.8° **b** 52.8° **c** 53.6° **d** 28.2°

11 **a** 8.13 cm **b** 32.3°

Area of a triangle using $\frac{1}{2}absinC$

Answers

12 a 18.1 cm²

b 18.7 cm²

c 693 mm²

13 5.10 cm

14 a 6.29 cm

b 84.3°

c 5.73 cm

d 58.8°

15 15.3 cm

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